

Physical constraints and biological regulations underlie universal osmoresponses

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Microorganisms constantly transition between environments with dramatically different external osmolarities. However, theories of microbial osmoresponse integrating physical constraints and biological regulations are lacking. Here, we propose such a theory, utilizing the separation of timescales for passive responses and active regulations. We demonstrate that regulations of osmolyte production and cell wall synthesis allow cells to adapt to a broad range of external osmolarity with a threshold value above which cells cannot grow, ubiquitous across bacteria and yeast. Intriguingly, the theory predicts a dramatic speedup of cell growth after an abrupt decrease in external osmolarity due to cell-wall synthesis regulation. Our theory rationalizes the unusually fast growth observed in fission yeast after an oscillatory osmotic perturbation, and the predicted growth rate peaks match quantitatively with experimental measurements. Our study reveals the physical basis of osmoresponse, yielding far-reaching implications for microbial physiology.

Microbes constantly transition between environments with dramatically different osmolarities, a hallmark of microbial life [1–4]. One of the most essential features of walled microbial cells is the turgor pressure — the elastic stress stretching the cell wall due to osmotic imbalance. Upon a hypoosmotic shock (i.e., a sudden decrease of the external osmolarity), the turgor pressure increases immediately due to the sudden water influx. To relax the turgor pressure, the cell up-regulates the cell-wall synthesis rate, adds more materials to the peptidoglycan network, and eventually adapts to the lower external osmolarity [5]. Upon a hyperosmotic shock (i.e., a sudden increase of the external osmolarity), the cell volume of a microbial cell shrinks within milliseconds due to water efflux, leading to a decreased turgor pressure [6, 7]. To increase the internal osmotic pressure, microorganisms increase their intracellular solute pool by amassing osmolyte molecules (i.e., osmoregulation), e.g., through *de novo* synthesis [8]. The cell volume then restores progressively over time, and eventually, the cell adapts to the higher osmolarity. Intracellular crowding may act as a cell volume sensor to trigger osmoregulation [9–11]. Meanwhile, intracellular crowding due to volume reduction inevitably affects the cellular physiology globally, e.g., slowing down protein diffusion [12–18] and reducing the elongation speed of translating ribosomes [19, 20]. Despite extensive knowledge regarding the molecular details of osmotic response pathways [4], how intracellular crowding interferes with gene expression regulation and affects osmotic adaption remains an open question.

Interestingly, many features of microbial osmoresponses appear general across different organisms, suggesting a universal underlying mechanism. For example, it is widely observed that microbial cells can adapt to a broad range of external osmolarity, with the external osmotic pressure varying over an order of magnitude [19, 21–23]. Furthermore, the growth rate in the steady state decreases as the external osmolarity increases and

a complete arrest of cell growth occurs above a critical osmolarity [19, 22–26]. Moreover, upon an osmotic shock, the growth rate usually does not approach the new steady-state value monotonically, e.g., an overshoot of growth rate often occurs upon a hypoosmotic shock [23], and a damped oscillation of growth rate can happen after a hyperosmotic shock [22]. In recent experiments of *Schizosaccharomyces pombe* [27], an oscillatory osmotic shock was applied to cells during which cell volume growth was dramatically slowed down while biomass was still actively produced. Surprisingly, a supergrowth phase happened after removing the oscillatory osmotic shock, during which cells grew much faster than the steady state before the shocks.

In this work, we unify all these phenomena by a theory capturing the essential elements of osmoresponses: physical constraints (e.g., the crowding effects and osmotic imbalance) and biological regulation, including osmoregulation (i.e., regulation of the osmolyte-producing protein) and cell-wall synthesis regulation. We apply nonequilibrium thermodynamics to model water flux across the cell membrane due to osmotic imbalance [7, 28]. We also introduce a coarse-grained model of proteome fraction, including the ribosomal proteins and osmolyte-producing protein [29]. Upon a hyperosmotic shock, cell volume reduction due to water efflux increases the protein density, inducing the up-regulation of osmolyte-producing protein but slowing down the translation speed due to crowding. Upon a hypoosmotic shock, the dramatic water influx stretches the cell wall, and the increased turgor pressure induces cell-wall synthesis [5, 30, 31].

We apply our theories to quantitatively fit the data of steady-state growth rate *vs.* internal osmotic pressure, from which we extract the sensitivities of the translation speed and regulation of osmolyte-producing protein to the intracellular density. We further demonstrate that osmoregulation and cell-wall synthesis regulation allow cells to adapt to a broad range of external osmolar-

ity and avoid plasmolysis. Further, our model predicts non-monotonic time dependence of growth rate and protein density towards the steady-state values after a constant osmotic shock, in concert with experimental observations [22, 23]. Moreover, we show that a super-growth phase can occur after the external osmolarity decreases abruptly due to cell-wall synthesis regulation. Remarkably, the predicted amplitudes of supergrowth (i.e., growth rate peaks) quantitatively match several independent experimental measurements.

RESULTS

Cell growth

In the limit of an extreme hyperosmotic shock, the remaining cytoplasmic volume is comparable to the volume of expelled water [14, 21, 32]. Thus, the total cytoplasmic volume must be divided into a free volume and a bound volume [28, 33–36],

$$V = V_f + V_b. \quad (1)$$

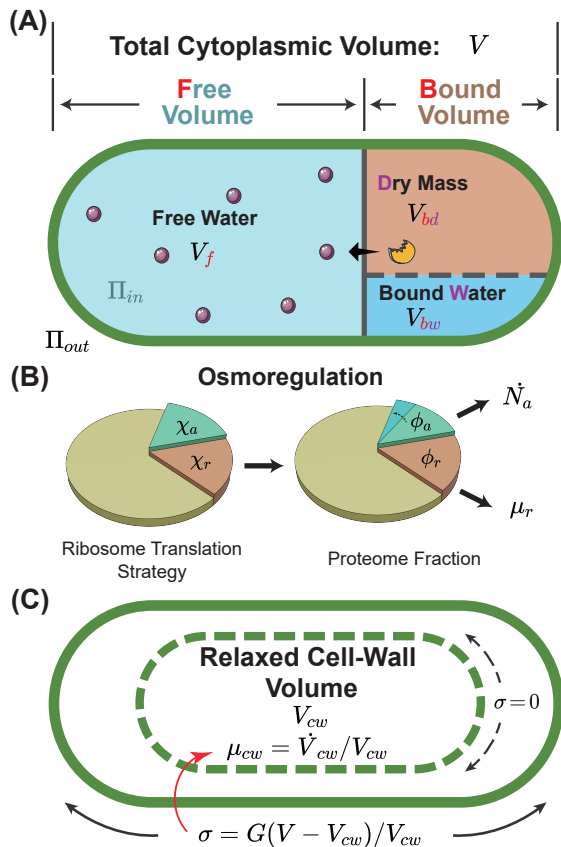


FIG. 1. A schematic of the osmoresponse model. (A) The total cytoplasmic volume includes the free and bound volumes. The free volume sets the internal osmotic pressure $\Pi_{in} = k_B T N_a / V_f$, where V_f is the free volume and N_a is the number of osmolyte molecules. The bound volume V_b comprises the dry mass V_{bd} and bound water V_{bw} , all proportional to the total protein mass. (B) We model osmoregulation through the change of ribosome translation strategy. When the protein density increases, the fraction of ribosomes translating the osmolyte-producing protein χ_a is up-regulated, leading to the subsequent increase in the mass fraction of the osmolyte-producing protein ϕ_a . (C) The cell-wall synthesis process is controlled by the turgor pressure σ , which is proportional to the cell-wall strain $\epsilon = (V - V_{cw})/V_{cw}$. Here, V is the cytoplasmic volume, and V_{cw} is the relaxed cell wall volume.

The free volume comes from the free water that is osmotically active, and the bound volume includes the bound water V_{bw} (i.e., water of macromolecular hydration) and the volume of dry mass V_{bd} (Figure 1A). Because the fraction of protein mass in the total dry mass is typically constant and the volume of bound water is proportional to the dry mass [21], the bound volume is proportional to the total protein mass m_p through $V_b = \alpha m_p$. Here, α is a constant, and its values for some model organisms are included in Table 1, and its detailed calculations from experimental data are in Section B of Supplementary Material.

The free volume changes due to osmotic imbalance, and the growth rate of the free volume follows

$$\mu_f \equiv \frac{\dot{V}_f}{V_f} = k_w (\Pi_{in} - \Pi_{out} - \sigma), \quad (2)$$

where Π_{in} , Π_{out} are the internal (i.e., cytoplasmic) and external osmotic pressures, respectively [7]. Π_{in} is proportional to the concentration of osmolyte molecules in the free volume: $\Pi_{in} = k_B T N_a / V_f$ where N_a is the number of osmolyte molecules, k_B is the Boltzmann constant, and T is the temperature. For simplicity, we assume that the production speed of osmolyte molecules is proportional to the mass of osmolyte-producing protein (Methods). Here, we have replaced the difference of the hydrostatic pressures across the cell membrane with the turgor pressure σ , assuming that mechanical equilibrium is always satisfied. k_w is the filtration coefficient quantifying the water permeability of the cell membrane [37].

The species of osmolytes involved in osmoregulation are diverse across different microorganisms and conditions; nevertheless, they are primarily small organic molecules [8, 38]. In this work, we simplify the problem by considering a single species of osmolyte that dominates the internal osmotic pressure, e.g., glycerol in *Saccharomyces cerevisiae* [39–41] and glycine betaine in *Escherichia coli* [3], with the production speed proportional to the mass of the osmolyte-producing protein (Figure 1A and Methods).

To model gene expression regulation, we introduce χ_a and χ_r as the fractions of ribosomes translating the osmolyte-producing protein and ribosomal proteins (Figure 1B and Methods). In steady states, χ_a and χ_r

151 are equal to the mass fractions of osmolyte-producing
152 protein and ribosomal proteins in the total proteome,
153 $\phi_a = m_{p,a}/m_p$ and $\phi_r = m_{p,r}/m_p$, respectively [29, 42].
154 In this work, we assume that the dry-mass growth rate
155 is proportional to the fraction of ribosomal proteins in
156 the proteome for simplicity, $\mu_r = k_r \phi_r$ where k_r is a con-
157 stant proportional to the elongation speed of ribosome.
158 The growth rate of the cytoplasmic volume, $\mu = \dot{V}/V$,
159 is a weighted average of the free-volume growth rate μ_f
160 and the dry-mass growth rate μ_r :

$$\mu = f\mu_f + (1-f)\mu_r. \quad (3)$$

161 Here, f is the free volume fraction in the total cytoplas-
162 mic volume: $f = V_f/V$. In this work, we refer to the
163 growth rate as the growth rate of cytoplasmic volume μ
164 unless otherwise mentioned.

165 Osmoregulation

166 Experiments found that the reduction of growth rate as
167 the external osmolarity increases is dominated by the re-
168 duction of the translation speed k_r , instead of the riboso-
169 mal fraction ϕ_r [19]. Therefore, we assume that the frac-
170 tion of ribosomes translating themselves χ_r is constant
171 for simplicity. To model osmoregulation, we introduce
172 a coupling between the fraction of ribosomes translating
173 the osmolyte-producing protein χ_a and the degree of in-
174 tracellular crowding. We quantify the crowding effects by
175 the protein density, defined as $\rho_p = m_p/V_f$, which serves
176 as a good proxy for the dry-mass density measured in
177 the experiments [43, 44] (see Table 1 and the detailed
178 discussion on the relations between the two densities in
179 Section A of Supplementary Material) and propose the
180 following relation:

$$\chi_a = \chi_a^{\max} \left(\frac{\rho_p}{\rho_c} \right)^{H_a}. \quad (4)$$

181 Here, the parameter H_a quantifies the sensitivity of os-
182 moregulation to intracellular crowding. χ_a^{\max} represents
183 the largest possible ϕ_a since all intracellular dynamics is
184 frozen when $\rho_p > \rho_c$.

185 Cell-wall synthesis regulation

186 The turgor pressure is proportional to the elastic strain
187 of the cell wall by an elastic modulus G such that

$$\sigma = G\epsilon = G \left(\frac{V}{V_{cw}} - 1 \right). \quad (5)$$

188 Here, V_{cw} is the relaxed cell-wall volume (Figure 1C).
189 When plasmolysis happens, the cell membrane detaches
190 from the cell wall ($V < V_{cw}$), and the turgor pressure

191 is zero. We introduce the growth rate of the relaxed
192 cell-wall volume as $\mu_{cw} = \dot{V}_{cw}/V_{cw}$. Given that in the
193 steady states of cell growth, $\mu_r = \mu_{cw}$, we write μ_{cw} in
194 the following form without losing generality,

$$\mu_{cw} = \mu_r \eta_{cw}. \quad (6)$$

195 Here, η_{cw} is a coarse-grained parameter modeling the ac-
196 tive regulation of cell-wall synthesis, which we refer to as
197 the cell-wall synthesis efficiency in the following.

198 Experiments suggested that the turgor pressure induce
199 cell-wall synthesis, e.g., through mechanosensors on cell
200 membrane [45, 46], by increasing the pore size of the pep-
201 tidoglycan network [5], and by accelerating the moving
202 velocity of the cell-wall synthesis machinery [31]. Guided
203 by these ideas, we model cell-wall synthesis regulation
204 through positive feedback from turgor pressure to the
205 cell-wall synthesis efficiency:

$$\dot{\eta}_{cw} = \frac{1}{\tau_{cw}^{\pm}} \left[\left(\frac{\sigma}{\sigma_c} \right)^{H_{cw}} - \eta_{cw} \right]. \quad (7)$$

206 Here, σ_c is a characteristic scale of turgor pressure de-
207 pending on species. τ_{cw}^+ (τ_{cw}^-) is the relaxation timescale
208 when the current η_{cw} is below (above) its target value
209 $\eta_{cw}^{st} = (\sigma/\sigma_c)^{H_{cw}}$. The former (latter) happens immedi-
210 ately after the cell is subject to a hypoosmotic (hyper-
211 osmotic) shock. In the extreme case of plasmolysis, the
212 insertion of newly synthesized cell wall materials is in-
213 terrupted immediately due to the separation of the cell
214 membrane and cell wall. Meanwhile, the up-regulation of
215 cell-wall synthesis rate presumably takes a longer time.
216 For example, in fungi, where polarized growth is gener-
217 ally adopted, the up-regulation of the cell-wall synthesis
218 rate involves reorienting the polarisome complex to the
219 growing tip, directing actin polarization, and delivering
220 cell-wall synthesis machinery [47, 48]. Therefore, we set
221 $\tau_{cw}^+ \gg \tau_{cw}^-$ in this work (see details of parameter values
222 in Table 1).

223 Intracellular crowding

224 Multiple experiments suggested the existence of a
225 glass transition in the cytoplasm of bacteria and yeast,
226 above which the cytoplasm freezes and the mobility of
227 biomolecules virtually stalls [14, 15, 49]. Intracellu-
228 lar crowding affects biochemical processes globally, e.g.,
229 slowing down translation and intracellular signaling by
230 suppressing protein diffusion [14, 15, 18, 19, 49]. There-
231 fore, the speed of osmolyte production, translational
232 elongation, and cell-wall synthesis are all slowed down
233 by the same crowding factor:

$$\eta_r = 1 - \left(\frac{\rho_p}{\rho_c} \right)^{H_r}. \quad (8)$$

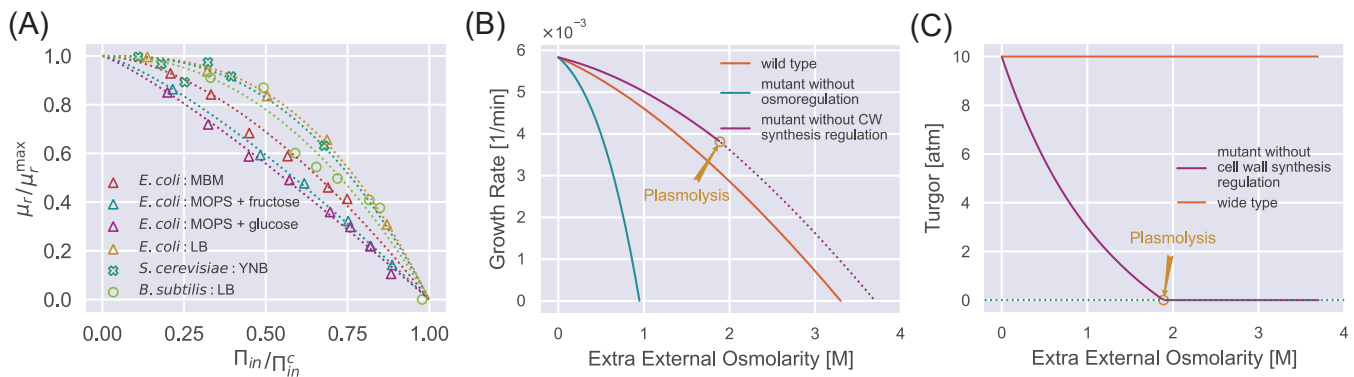


FIG. 2. Steady-state properties under a constant external osmolarity. (A) Normalized growth rate vs. normalized internal osmotic pressure of different species under various culture media. The experiment data (scatter markers) are fitted by our theoretical prediction Eq. (10b). The data of *E. coli* are from [19, 21, 22], the data of *B. subtilis* is from [23], and the data of *S. cerevisiae* is from our own experiments. (B) Growth curves of WT cells, mutant cells without osmoregulation ($H_a = 0$), and mutant cells without cell-wall synthesis regulation ($H_{cw} = 0$). The dotted line indicates the region where plasmolysis occurs for the mutant cells with $H_{cw} = 0$. (C) Mutant cells without cell-wall synthesis regulation cannot maintain a stable turgor pressure in a hypertonic environment, while WT cells can maintain a constant turgor pressure. The mutant cells reach plasmolysis at a threshold of external osmolarity. In (B) and (C), the parameters for WT cells are chosen as the values for *S. pombe*, and the mutant values are set such that they have the same growth rate as the WT cells in the reference medium (Table S2).

234 Here, ρ_c is the critical protein density, and H_r is a parameter to quantify the sensitivity of biochemical reactions to the intracellular density. For example, the translational elongation speed is suppressed by intracellular crowding through $k_r = k_r^{\max} \eta_r$. Therefore, the dry-mass growth rate becomes $\mu_r = \mu_r^{\max} \eta_r$, where we introduce $\mu_r^{\max} = k_r^{\max} \phi_r$.

241 The details of our model are summarized in Methods, with five independent variables: the protein density ρ_p , the mass fraction of osmolyte-producing protein ϕ_a , the internal osmotic pressure Π_{in} , the cell-wall strain ϵ and the cell-wall synthesis efficiency η_{cw} .

246 Steady states in constant environments

247 All growth rates in steady states of cell growth are the same: $\mu_f = \mu_r = \mu_{cw}$. The consequence of cell-wall synthesis regulation can be seen directly from $\mu_{cw} = \mu_r$: the turgor pressure at steady states is constant, $\sigma = \sigma_c$. Experimentally, the cell-wall strain was measured by applying an acute hyperosmotic shock to induce plasmolysis, and it is approximately constant as the external osmolarity increases [22, 50], suggesting a constant turgor pressure independent of external osmolarity, in concert with our model assumptions. The internal osmotic pressure at steady states is related to the external osmotic pressure through Eq. (2),

$$\Pi_{in} = \Pi_{out} + \sigma. \quad (9)$$

259 Here, we have neglected the term μ_f/k_w . Experimentally, an abrupt water flux occurs within hundreds of milliseconds after an osmotic shock [51], from

262 which we can estimate the water permeability as $k_w \sim 100 \text{ min}^{-1} \text{ atm}^{-1}$ considering an osmotic shock with an amplitude $\Delta \Pi_{out} = 1 \text{ atm}$. Because the typical doubling times of microorganisms are around hours, we can estimate $\mu_f/k_w \sim 10 \text{ Pa}$ [51, 52], negligible compared with the typical cytoplasmic osmotic pressures, which can be several atmospheric pressures.

269 In steady states, the internal osmotic pressure is independent of time. Combining Eq. (4) and the dynamics of the internal osmotic pressure, Eq. (18c), we find the relationships between the protein density, the internal osmotic pressure, and the growth rate in the steady states:

$$\frac{\Pi_{in}}{\rho_p^{H_a+1}} = \text{const}, \quad (10a)$$

$$\frac{\mu_r}{\mu_r^{\max}} = 1 - \left(\frac{\Pi_{in}}{\Pi_{in,c}} \right)^{\frac{H_r}{H_a+1}}. \quad (10b)$$

274 The right-hand side of Eq. (10a) is a constant independent of external osmolarity (see its detailed expression in Section C of Supplementary Material). In deriving Eq. (10b), we have replaced ρ_p by Π_{in} in Eq. (8) using Eq. (10a) with the critical internal osmotic pressure $\Pi_{in,c}$ proportional to ρ_c . Intriguingly, the universal relationship between the normalized growth rate and the normalized Π_{in} , which we refer to as the growth curve in the following, has only one degree of freedom $H_r/(H_a + 1)$. Eq. (10b) predicts a critical external osmolarity $\Pi_{out,c} = \Pi_{in,c} - \sigma_c$, beyond which cell growth is completely inhibited.

286 We test the validity of Eq. (10b) by fitting it to the experimental growth curves (Figure 2A). To do this, we calculate the internal osmotic pressure using Eq. (9) given

the values of the external osmotic pressure and the turgor pressure (Table 1). Intriguingly, the growth curves of multiple species can be well fitted by Eq. (10b), from which we infer the parameters $H_r/(H_a + 1)$ and $\Pi_{in,c}$ (Table 1). We find that budding yeast cells exhibit a notable resilience to high external osmolarities: their $\Pi_{in,c}$ value is higher than those of Gram-positive bacteria, *B. subtilis*, and Gram-negative bacteria, *E. coli*. Further, budding yeast cells demonstrate a higher value of $H_r/(H_a + 1)$, indicating a reduced susceptibility to growth rate reduction when exposed to mild increases in the external osmolarity. Meanwhile, the osmoadaptation capability of *E. coli* depends on the growth media, presumably arising from variations in metabolic fluxes and gene expressions [19, 21, 22].

To further reveal the biological functions of biological regulations, we study the steady-state properties of mutant cells in which either osmoregulation or cell-wall synthesis regulation is depleted. For mutant cells without osmoregulation, $H_a = 0$ in Eq. (4). In this case, the fraction of osmolyte-producing protein is constant with time, i.e., $\phi_a = \chi_a^{\max}$. Comparing the dynamics of osmolyte and total protein mass, $\dot{N}_a = k_a \phi_a m_p$ and $\dot{m}_p = k_r \phi_r m_p$, one finds that the ratio of the number of osmolyte molecule and the total protein mass remains constant over time, irrespective of variations in external osmolarity (see the detailed derivation in Section C of Supplementary Material). As the external osmolarity increases, the protein density of mutant cells quickly reaches the critical value ρ_c according to Eq. (10a) with $H_a = 0$. Therefore, the steady-state growth curve of the mutant cells terminates at an external osmolarity much smaller than wild-type (WT) cells (Figure 2B), in agreement with previous experiments [53].

For mutant cells without the cell-wall synthesis regulation, $H_{cw} = 0$; therefore, the cell-wall synthesis efficiency η_{cw} equals 1 independent of time. Thus, the growth rate of the relaxed cell-wall volume is always equal to the growth rate of total protein mass [Eqs. (6, 7)]. Interestingly, in this case, the turgor pressure at steady states decreases with the increase of external osmolarity (Figure 2C and see the detailed proof in Section C of Supplementary Material). The decreased turgor pressure lowers the internal osmotic pressure given the same Π_{out} according to Eq. (9), leading to a lower protein density of mutant cells than WT cells according to Eq. (10a). Therefore, mutant cells grow faster than WT cells under the same external osmolarity (Figure 2B). Nevertheless, the mutant cells are prone to plasmolysis at a threshold external osmolarity where the WT cells can maintain constant turgor pressure (see the vertical line in Figure 2C around 2 M extra external osmolarity). Reduced turgor pressure is detrimental to multiple biological processes, e.g., cytokinesis in fission yeast requires the participation of turgor pressure [54].

To summarize, osmoregulation allows cells to grow in a

wide range of external osmolarity conditions with a mild change in protein density. The cell-wall synthesis regulation allows cells to maintain a stable turgor pressure and avoid plasmolysis. Both regulatory mechanisms expand the range of external osmolarities that cells can adapt to.

350 Transient dynamics after a constant osmotic shock

351 Next, we study the dynamical behaviors of cellular
352 properties in response to a constant osmotic shock: the
353 external osmolarity changes abruptly and keeps its value
354 for an infinitely long time. Intriguingly, we find that
355 the dynamics of osmoresponse can be split into shock
356 and adaptation periods (see insets of Figure 3C, D).
357 The immediate water flow due to osmotic imbalance oc-
358 curs in the shock period, during which the mass and os-
359 molyte productions are negligible. Therefore, the ratio
360 of the internal osmotic pressure and the protein den-
361 sity is invariant right before and after a shock period:
362 $\Pi_{in}^i/\rho_p^i = \Pi_{in}^f/\rho_p^f$ where the upper index i (f) means the
363 state right before (after) the shock period. Given this
364 condition, we introduce the normalized protein density
365 $\tilde{\rho}_p$ as

$$\tilde{\rho}_p = \frac{\rho_p}{\bar{\rho}_p}, \quad (11)$$

366 where the normalization factor $\bar{\rho}_p \propto \Pi_{in}$ (see its detailed
367 expression in Methods) so that $\tilde{\rho}_p$ changes continuously
368 across the shock period. Interestingly, we find that os-
369 moresponse are governed by a two-dimensional dynam-
370 ical system composed of $\tilde{\rho}_p$ and $\eta_a \equiv \phi_a/\chi_a^{\max}$ (Methods):

$$\frac{\dot{\tilde{\rho}}_p}{\tilde{\rho}_p} = \mu_r^{\max} \eta_r (1 - \tilde{\rho}_p \eta_a). \quad (12a)$$

$$\dot{\eta}_a = \mu_r^{\max} \eta_r \left[\left(\frac{\tilde{\rho}_p}{\tilde{\rho}_c} \right)^{H_a} - \eta_a \right], \quad (12b)$$

371 Here, $\tilde{\rho}_c = \rho_c/\bar{\rho}_p$ is the normalized critical protein den-
372 sity, and η_a denotes the efficiency of osmoregulation.
373 From the above equations, it is clear that the timescale of
374 osmoregulation is set by the doubling time: it takes about
375 the doubling time for the protein density and the frac-
376 tion of osmolyte-producing protein to adapt to the new
377 steady-state values. For walled cells, $\tilde{\rho}_c$ and $\bar{\rho}_p$ depend
378 on the time since $\Pi_{in} = \Pi_{out} + \sigma$ and the turgor pressure
379 σ is time-dependent during osmoresponse processes (Fig-
380 ure 3A, B). For unwalled cells, such as mammalian cells
381 and microbial cells with cell walls removed (i.e., proto-
382 plasts), $\tilde{\rho}_c$ is constant in a fixed environment (see detailed
383 discussion on the transient dynamics of unwalled cells in
384 Section D of Supplementary Material).

385 Upon a constant hyperosmotic shock, the immediate
386 water efflux leads to an instantaneous drop in turgor
387 pressure and a rise in protein density (Figure 3A). The

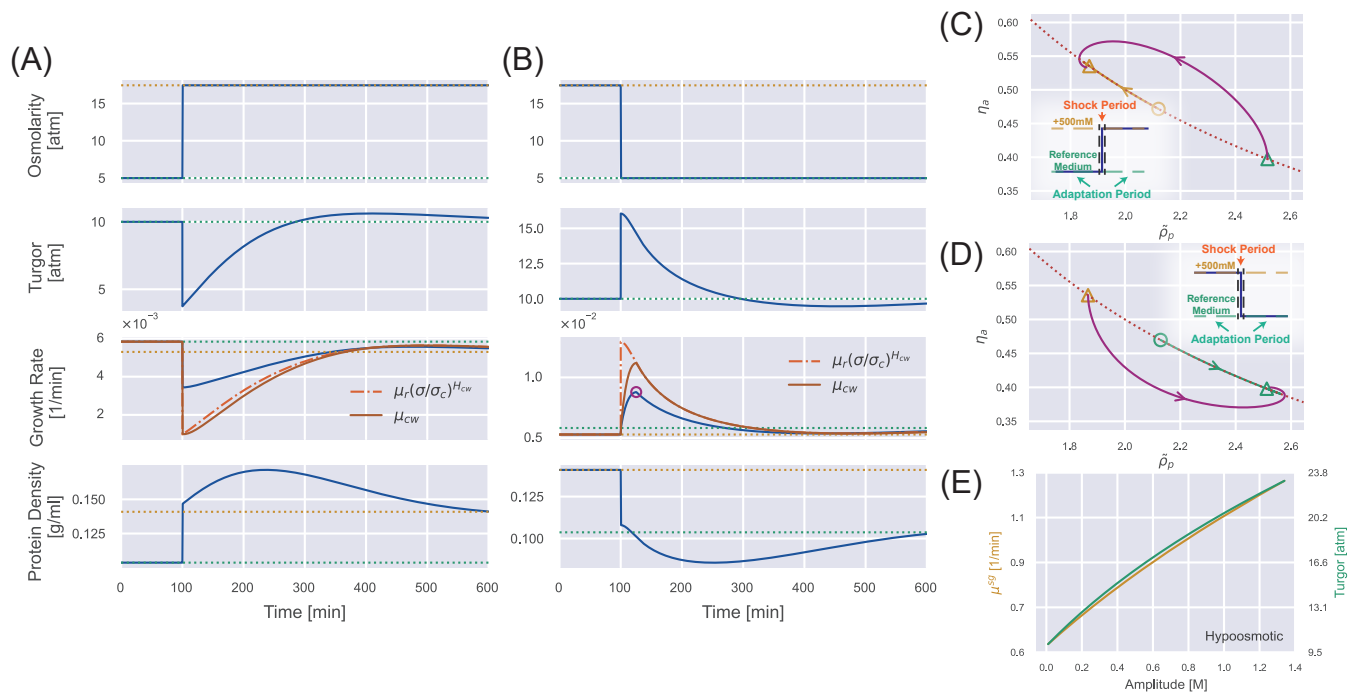


FIG. 3. **Transient dynamics after a constant osmotic shock.** (A) Numerical simulations of cells undergoing a constant 500 mM hyperosmotic shock. The dotted lines represent the steady-state values for the reference growth medium (green) and the medium after perturbation (yellow). (B) Numerical simulations of cells undergoing a constant 500 mM hypoosmotic shock. The purple circle in the third panel marks the growth rate peak during the supergrowth phase. The dotted curve represents the constraint on the steady-state solution $\tilde{\rho}_p \eta_a = 1$, and the solid trajectory is from numerical simulations. The triangles indicate the steady-state solution before the perturbation and the steady-state solution after the perturbation for a long enough time. The yellow open circle represents the immediate steady-state solution after applying the hyperosmotic shock. (D) The same analysis as (C) but for a constant 500 mM hypoosmotic shock. (E) The growth rate peak in the supergrowth phase (yellow) and the immediate value of turgor pressure after the hypoosmotic shock σ^J (green) vs. the amplitude of the hypoosmotic shock.

388 internal state of the cell, $(\tilde{\rho}_p, \eta_a)$ evolves towards to the
 389 new equilibrium point, $(\tilde{\rho}_c^{H_a/(H_a+1)}, \tilde{\rho}_c^{-H_a/(H_a+1)})$. One
 390 should note that the equilibrium point is time-dependent
 391 initially but eventually becomes fixed as the turgor pres-
 392 sure relaxes to the steady-state value (Figure 3C and
 393 Movie S1). Interestingly, the protein density increases
 394 initially and then decreases after the shock (Figure 3A).
 395 The decrease in protein density is because of the os-
 396 moregulation process, which is set by the doubling time
 397 [Eqs. (12a, 12b)]. Meanwhile, we find that the initial
 398 increase of protein density is because of the suppressed
 399 growth of the relaxed cell-wall volume due to the low
 400 turgor pressure. Indeed, for unwalled cells, the protein
 401 density ρ_p decreases immediately after the shock (Fig-
 402 ure S2B). We note that the growth rate approaches the
 403 new steady-state value non-monotonically (Figure 3A)
 404 because of the spiral trajectory in the space of the in-
 405 ternal state (Figure 3C), consistent with experimental
 406 observations [22].

407 The phenomena are essentially the opposite for a con-
 408 stant hypoosmotic shock (Figure 3B, D and Movie S2).
 409 However, we find an extremely fast cell growth after the

410 hypoosmotic shock, with a growth rate peak occurring
 411 about 25 minutes after applying the shock, which we call
 412 the supergrowth phase [27]. One should note that 25 min-
 413 utes is much shorter than the doubling time (about two
 414 hours) but comparable to the timescale of cell-wall syn-
 415 thesis regulation, which we set as $\tau_{cw}^+ = 12.5$ min in the
 416 simulations in Figure 3 (we will explain why we choose
 417 $\tau_{cw}^+ = 12.5$ min in the next section). Furthermore, ap-
 418 plying a hypoosmotic shock to an unwalled cell does not
 419 induce a significant supergrowth phase compared with
 420 walled cells (Figure S2D).

421 We propose that supergrowth comes from the high tur-
 422 gor pressure caused by the hypoosmotic shock, which
 423 leads to a fast cell-wall synthesis according to Eq. (7).
 424 Rapid insertion of materials into the cell wall relaxes
 425 the turgor pressure and allows the cells to grow faster
 426 [Eqs. (2, 3)]. This idea is consistent with the observa-
 427 tion that the growth rate and the growth rate of the
 428 relaxed cell-wall volume μ_{cw} reach their peaks simulta-
 429 neously (Figure 3B). This observation also suggests that
 430 the timescale of supergrowth, i.e., the timing of growth
 431 rate peak, is set by the time scale of cell-wall synthesis

regulation [τ_{cw}^+ in Eq. (7)]. Notably, in the initial stage of the adaptation period, μ_{cw} approaches its target from below and reaches its target value at the growth rate peak (i.e., $\mu_r(\sigma/\sigma_c)^{H_{cw}}$) (the third panel of Figure 3B), after which μ_{cw} sticks to its target value and decreases accordingly because of the short relaxation time τ_{cw}^- [Eq. (7)]. A detailed proof of the conditions for supergrowth, including the necessity of a cell wall and the regulation of cell-wall synthesis, is provided in Section E of the Supplementary Material.

Following the discussion above, we obtain an analytical expression of the growth rate peak after a hypoosmotic shock (see the detailed derivations in Section F of Supplementary Material)

$$\mu^{sg} = \mu_r \left\{ 1 + \frac{f}{f + \frac{\Pi_{in}}{\sigma + G}} \times \left[\left(\frac{\sigma}{\sigma_c} \right)^{H_{cw}} - 1 \right] \right\}. \quad (13)$$

Here, all the variables on the right side are at the growth rate peak. Because the timescale of the osmoreponse process, which is around hours (Figure 3B), is much longer than the timescale of the supergrowth phase, which is about 20 minutes, the turgor pressure at the growth rate peak can be well approximated by its immediate value after the shock. Therefore, the growth rate peak must increase as the amplitude of the hypoosmotic shock increases, which we confirm numerically (Figure 3E).

Comparison between theories and experiments

Next, we quantitatively compare our theoretical predictions regarding the supergrowth phase with experimental data. In Ref. [27], Knapp et al. applied an osmotic oscillation to fission yeast *S. pombe* during which the external osmolarity alternated between two values. They found cell growth was almost inhibited during the perturbation, while the protein and dry-mass densities increased. Surprisingly, cells grew unusually fast after the osmotic oscillation was removed and reached their maximum growth rate about 20 minutes after the end of the osmotic oscillation. The maximum growth rate can be twice the growth rate in the reference growth medium, and the elevation in growth rate can persist for 2-3 cell cycles. These observations are very similar to our results for a constant hypoosmotic shock (Figure 3B).

To test if our osmoreponse model captures the supergrowth phase for a periodic perturbation, we simulate a wide-type *S. pombe* cells with the same protocols as the experiments (see details of simulations in Methods). Intriguingly, our model successfully recapitulates the supergrowth phase and the gradually increasing protein density and dry-mass density during the perturbation (Figure 4A). We confirm that the cell-wall synthesis regulation is crucial for the emergence of the supergrowth

phase since unwallled cells do not exhibit supergrowth under the same conditions (Figure S3B). Interestingly, we find that an infinitely long periodic osmotic shock can be equivalently mapped to a constant osmotic shock (see the detailed discussions and proof in Section D of Supplementary Material), which means that they have the same time-averaged growth rate and protein density in the steady states (Figure S2F).

In Ref. [27], the authors measured the growth rate peaks vs. three different parameters of the osmotic oscillations: amplitude, period length, and number of periods. We first fit the growth rate peaks vs. the amplitudes (Figure 4D), from which we obtain $H_{cw} = 1.7$, the sensitivity of the cell-wall synthesis efficiency to turgor pressure [Eq. (7)], and $\tau_{cw}^+ = 12.5$ min, the timescale in the up-regulation of cell-wall synthesis efficiency (which is why we set $\tau_{cw}^+ = 12.5$ min in the previous section). Other model parameters are inferred from independent steady-state measurements, and we set the timescale in the down-regulation of cell-wall synthesis efficiency as $\tau_{cw}^- = 0.1$ min for simplicity (Table 1). We next fix the values of H_{cw} and τ_{cw}^+ and plot the predicted growth rate peaks vs. the period length (Figure 4B) and number of periods (Figure 4C). As a strong support of our model, our predictions quantitatively match the experimental data without any further fitting.

Two interesting features of the curve μ^{sg} v.s amplitude catch our attention: the non-monotonic behavior and the kink point at which the derivative is discontinuous (Figure 4D), which are conserved regardless of the number of periods (Figure S7). Therefore, we study the case of a single oscillation for simplicity, which is equivalent to a hyperosmotic shock of finite duration. For a mild hyperosmotic shock, during the period of hyperosmotic shock, the turgor pressure has almost recovered to the steady-state value σ_c (Figure 3A). Therefore, switching from a long hyperosmotic period to the reference growth medium is equivalent to a constant hypoosmotic shock, where we have shown that the growth rate peak increases with the amplitude (Figure 3E). However, the crowding effect becomes more pronounced as the amplitude increases. Beyond the critical amplitude at the kink point, the cytoplasm is completely jammed during the hyperosmotic shock such that the cell states are precisely the same before and after the hyperosmotic shock, which means no supergrowth phase beyond this critical amplitude. Therefore, the curve μ^{sg} vs. amplitude must be non-monotonic (Figure 4E). Notably, for a very large H_r , cells can feel the crowding effect only when the cytoplasm is close enough to the critical protein density, shown as the abrupt decline of μ^{sg} (Figure 4F).

Finally, we remark that the significance of supergrowth is intimately related to the amount of recovered turgor pressure during the hyperosmotic shock $\delta\sigma$. We prove that the overshoot of turgor pressure after the removal of hyperosmotic shock ($\sigma^f - \sigma_c$), which sets the growth

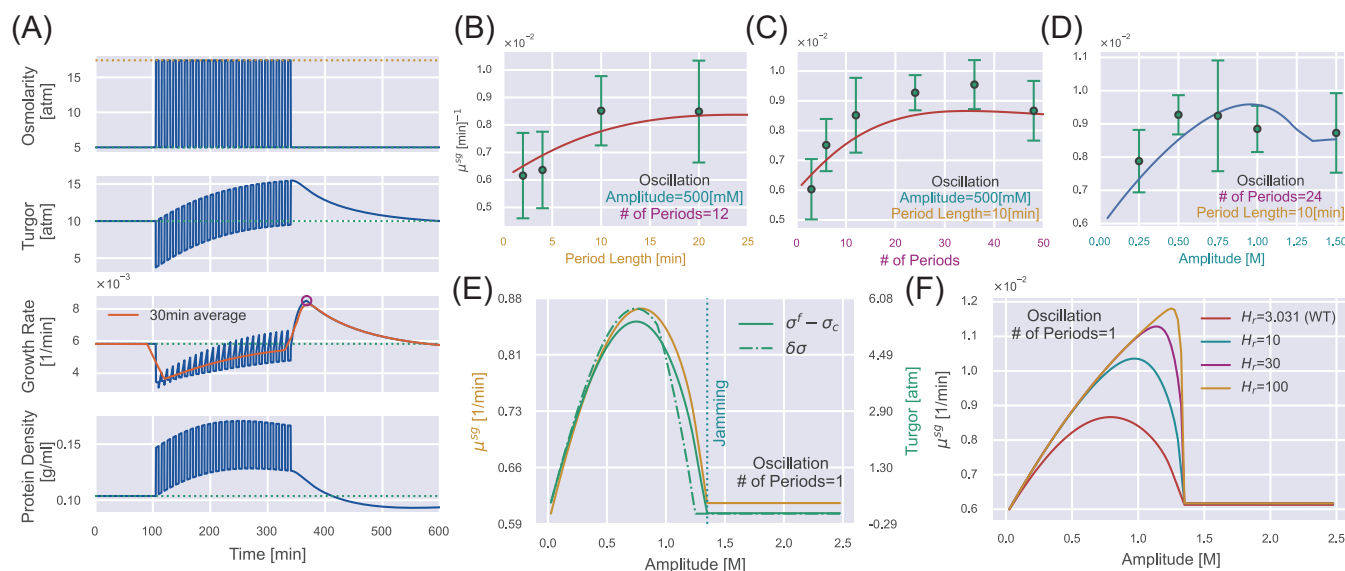


FIG. 4. Comparison between theories and experiments. (A) Numerical simulations of WT *S. pombe* undergoes 24 cycles of 500 mM osmotic oscillations with a 10-minute period. We show a 30-minute window average in the third panel of growth rate. (B-D) Quantitative agreement between simulations and experiments for the growth rate peak μ^{sg} vs. different oscillation parameters, including (B) amplitude, (C) period length, and (D) number of periods. The red lines in (B, C) are predictions, and the blue line in (D) is fitting from which we infer the values of H_{cw} and τ_{cw}^+ . Green dots with error bars are experimental data from Ref. [27]. (E) In the case of osmotic oscillation with a single period, the hyperosmotic period persists for 120 min before reverting to the reference medium. The vertical dotted blue line represents the minimal amplitude to induce cytoplasm jamming during the hyperosmotic period. The excess turgor pressure $\sigma^f - \sigma_c$ upon exiting the hyperosmotic period is approximately equal to the recovered turgor pressure $\delta\sigma$ during the hyperosmotic period. (F) The growth rate peak μ^{sg} at different H_r vs. the amplitude of a single oscillation. $H_r = 3.031$ is the value of the WT *S. pombe*. Parameters of WT *S. pombe* are used in this figure unless otherwise mentioned (Table 1).

537 rate peak, is mainly set by the recovered turgor pressure
 538 during the hyperosmotic shock (see the detailed discus-
 539 sions in Section G of Supplementary Material). Indeed,
 540 μ^{sg} , $\sigma^f - \sigma_c$, and $\delta\sigma$ are highly correlated as we change
 541 the amplitude (Figure 4E).

DISCUSSIONS

543 This study presents a theory of microbial osmore-
 544 sponses based on a physical foundation and simplified bi-
 545 ological regulation strategies. Regarding the steady-state
 546 properties, our theory successfully recapitulates the con-
 547 stant turgor pressure and the growth rate reduction as
 548 the external osmolarity increases. In particular, we pre-
 549 dict a critical external osmolarity above which cell growth
 550 is completely inhibited and a universal relationship be-
 551 tween the normalized growth rate and the normalized
 552 internal osmotic pressure, which nicely fits the data of
 553 bacteria and yeast. We also demonstrate the biological
 554 functions of osmoregulation and cell-wall synthesis reg-
 555 ulation. Cells defective in osmoregulation cannot grow
 556 even if the external osmolarity is only mildly higher than
 557 the reference value. Cells defective in cell-wall synthesis
 558 regulation cannot maintain turgor pressure as the exter-

559 nal osmolarity increases even though they grow faster
 560 than WT cells (Figure 2B), which will be a strong sup-
 561 port of our theory if confirmed by experiments.

562 Regarding dynamic behaviors, our model predicts a
 563 non-monotonic time dependence of protein density after
 564 a constant hyperosmotic shock. We also unveil the super-
 565 growth phase after a hypoosmotic shock, initially discov-
 566 ered in fission yeast after an osmotic oscillation [27]. As
 567 a strong support of our theory, the predicted growth rate
 568 peaks quantitatively agree with the experimental data
 569 without additional fitting. We demonstrate the critical
 570 role of cell-wall synthesis regulation in the supergrowth
 571 phenomenon (Section E of Supplementary Material). In
 572 Ref. [27], the authors observed the rapid repolarization
 573 of the cell-wall glucan synthase Bgs4 to the cell tip fol-
 574 lowing the removal of osmotic oscillations in fission yeast,
 575 in agreement with the dynamics of the cell-wall synthesis
 576 efficiency predicted from our model (compare Figure S11
 577 in this work and Figure S4H in Ref. [27]). To test our
 578 theories, we propose applying a hyperosmotic shock with
 579 a finite duration and measuring the growth rate after
 580 removing the hyperosmotic shock. We predict that the
 581 growth rate peak during the supergrowth phase is a non-
 582 monotonic function of the shock amplitude (Figure 4E).

583 Ref. [22] showed that the expansion of *E. coli* cell wall

is not directly regulated by turgor pressure, a scenario akin to $H_{cw} = 0$ in our model. According to our model, the supergrowth phase is absent if $H_{cw} = 0$ (Figure S8), consistent with the absence of a growth rate peak after a hypoosmotic shock in the experiments of *E. coli* [22]. Our predictions are also consistent with the growth rate peak after a hypoosmotic shock observed for *B. subtilis* [23]. Nevertheless, the growth inhibition before the peak, as observed in Ref. [23], which may be due to the high membrane tension that inhibits transmembrane flux of peptidoglycan precursors, is beyond our model.

In our current framework, the osmoregulation and cell-wall synthesis regulation relies on the instantaneous cellular states: protein density and turgor pressure. However, microorganisms can exhibit memory effects to external stimuli by adapting to their temporal order of appearance [55]. Notably, in the osmoregulation of yeast, a short-term memory, facilitated by post-translational regulation of the trehalose metabolism pathway, and a long-term memory, orchestrated by transcription factors and mRNP granules, have been identified [56]. Besides, our model does not account for the role of osmolyte export in osmoregulation, which has been shown to help cells recover from a sudden drop in external osmolarity [57]. Exploring the interference between osmolyte export and the supergrowth phase will be interesting.

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METHODS

Details of the osmoreponse model

We define the fractions of osmolyte-producing protein and ribosomal proteins in the total proteome as $\phi_a = m_{p,a}/m_p$ and $\phi_r = m_{p,r}/m_p$, respectively. To model gene expression regulation, we introduce χ_a and χ_r as the fractions of ribosomes translating the osmolyte-producing protein and ribosomal proteins such that

$$\dot{m}_{p,r} = k_r \chi_r m_{p,r} \Rightarrow \dot{\phi}_r = k_r \phi_r (\chi_r - \phi_r), \quad (14)$$

$$\dot{m}_{p,a} = k_r \chi_a m_{p,r} \Rightarrow \dot{\phi}_a = k_r \phi_r (\chi_a - \phi_a), \quad (15)$$

$$\dot{m}_p = k_r m_{p,r} \Rightarrow \mu_r = k_r \phi_r. \quad (16)$$

Here, k_r equals the elongation speed of ribosomes on mRNAs divided by the protein mass of a single ribosome, which is affected by the global crowding effect as

$k_r = k_r^{\max} \eta_r$. Here, μ_r is the growth rate of total protein mass, which is also the growth rate of dry mass and bound volume in our model since they are all proportional.

The osmolyte molecules are produced by the osmolyte-producing protein, with the rate given by

$$\dot{N}_a = k_a m_{p,a}, \quad (17)$$

where $k_a = k_a^{\max} \eta_r$ is the osmolyte production rate including the crowding factor and $m_{p,a}$ is the mass of osmolyte-producing protein. We summarize the dynamical equations involved in the osmoreponse model:

$$\dot{\rho}_p = (\mu_r - \mu_f) \rho_p \quad (18a)$$

$$\dot{\eta}_a = \mu_r \left[\left(\frac{\rho_p}{\rho_c} \right)^{H_a} - \eta_a \right] \quad (18b)$$

$$\dot{\Pi}_{in} = k_B T k_a^{\max} \eta_r \phi_a \rho_p - \mu_f \Pi_{in} \quad (18c)$$

$$\dot{\epsilon} = (\mu - \mu_{cw})(\epsilon + 1) \quad (18d)$$

$$\dot{\eta}_{cw} = \frac{1}{\tau_{cw}^{\pm}} \left[\left(\frac{\sigma}{\sigma_c} \right)^{H_{cw}} - \eta_{cw} \right]. \quad (18e)$$

To describe the osmoregulation process using a two-dimensional dynamical system, we introduce the normalized protein density as

$$\tilde{\rho}_p = \frac{k_B T k_a^{\max} \chi_a^{\max} \rho_p}{\mu_r^{\max} \Pi_{in}} \equiv \frac{\rho_p}{\bar{\rho}_p}, \quad (19)$$

Combining Eq. (11) and Eq. (18a), we obtain the dynamical equation for $\tilde{\rho}_p$ as

$$\frac{\dot{\tilde{\rho}}_p}{\tilde{\rho}_p} = \mu_r^{\max} \eta_r (1 - \tilde{\rho}_p \eta_a). \quad (20)$$

Using Eq. (15), we obtain the equation for $\eta_a = \phi_a / \chi_a^{\max}$

$$\dot{\eta}_a = \mu_r^{\max} \eta_r \left[\left(\frac{\tilde{\rho}_p}{\tilde{\rho}_c} \right)^{H_a} - \eta_a \right], \quad (21)$$

where $\tilde{\rho}_c = \rho_c / \bar{\rho}_p$. The unique equilibrium point for the internal state is

$$(\tilde{\rho}_p^{eq}, \eta_a^{eq}) = \left(\tilde{\rho}_c^{\frac{H_a}{H_a+1}}, \tilde{\rho}_c^{-\frac{H_a}{H_a+1}} \right). \quad (22)$$

Details of numerical simulations

We employ the LSODA algorithm with automatic stiffness detection and switching [59], implemented in SciPy [60], to solve Eq. (18). The parameters used for numerical simulations of walled cells are listed in Table 1.

E. coli	Value	Reference
σ_c	1 [atm]	Ref. [6]
α	1.68 [ml/g]	Deduce from Ref. [32] (see Supplementary Material)
	MBM [21]	MOPS+fructose [19] MOPS+glucose [19] LB [22]
$k_r^{\max} \chi_r$	0.743 [1/h]	0.776 [1/h] 1.14 [1/h] 2.05 [1/h]
$\Pi_{in,c}$	1.54 [Osm]	1.49 [Osm] 1.61 [Osm] 2.18 [Osm]
$H_r/(H_a + 1)$	1.68	1.30 1.18 2.72
<hr/>		
B. subtilis (LB)	Value	Reference
σ_c	19 [atm]	Ref. [33]
$k_r^{\max} \chi_r$	2.52 [1/h]	Fit to Ref. [23]
$\Pi_{in,c}$	3.09 [Osm]	
$H_r/(H_a + 1)$	2.18	
<hr/>		
S. cerevisiae (YPD)	Value	Reference
Π_{out}	0.26 [Osm]	
σ_c	3.1 [atm]	Ref. [35]
$\hat{\rho}_d$	0.295 [g/ml]	Ref. [43]
μ	0.448 [1/h]	Our experiment
f	0.6	Ref. [14]
ρ_p	0.155 [g/ml]	See Supplementary Material
ρ_c	0.994 [g/ml]	See Supplementary Material
α	4.29 [ml/g]	See Supplementary Material
$k_r^{\max} \chi_r$	0.450 [1/h]	Fit to our data
$\Pi_{in,c}$	3.52 [Osm]	
$H_r/(H_a + 1)$	2.54	
H_r	3.03	Set according to $1 - (\rho_p/\rho_c)^{H_r} = \mu/k_r^{\max} \chi_r$
<hr/>		
S. pombe (YE5S)	Value	Reference
Π_{out}	0.2 [Osm]	Ref. [58]
σ_c	10 [atm]	Ref. [35]
$\hat{\rho}_d$	0.282 [g/ml]	Ref. [44]
ρ_p	0.104 [g/ml]	See Supplementary Material
μ	0.35 [1/h]	Ref. [27]
f	0.788	Fit to Ref. [18] (see Supplementary Material)
ϵ	0.584	Ref. [58]
α	2.60 [ml/g]	See Supplementary Material
G	17.1 [atm]	$G = \sigma/\epsilon$
$\Pi_{out,c}$	3.5 [Osm]	
k_w	100 [1/(min atm)]	
ρ_c	0.267 [g/ml]	Deduce from Ref. [18] (see Supplementary Material)
H_r	3.03	Copied from <i>S. cerevisiae</i> in YPD
H_a	0.974	Set according to $\Pi_{in}/\Pi_{in,c} = (\rho_p/\rho_c)^{H_a}$
$k_r^{\max} \chi_r$	0.371 [1/h]	Set according to $\mu_r = k_r^{\max} \chi_r \left(1 - (\rho_p/\rho_c)^{H_r}\right)$
$k_B T k_a^{\max} \chi_a^{\max}$	2.25 [(atm ml)/(g min)]	Set according to $k_B T k_a^{\max} \chi_a^{\max} \eta_a \rho_p = k_r^{\max} \chi_r \Pi_{in}$
τ_{cw}^-	0.1 [min]	
τ_{cw}^+	12.5 [min]	Fit to Ref. [27]
H_{cw}	1.7	

TABLE 1. Model parameters for different species in their corresponding reference growth media.

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